

# The Consequences of Unobserved Heterogeneity in a Sequential Logit Model

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# Introduction

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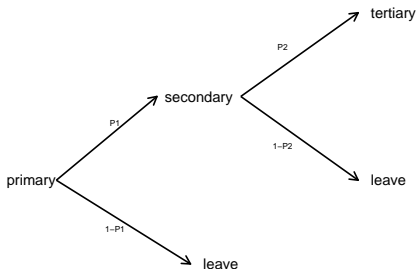
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- ▶ This model has been re-invented many times and is known under many names:
  - ▶ sequential logit model (Tutz 1991)
  - ▶ sequential response model (maddala 1983),
  - ▶ continuation ratio logit (Agresti 2002),
  - ▶ model for nested dichotomies (fox 1997), and
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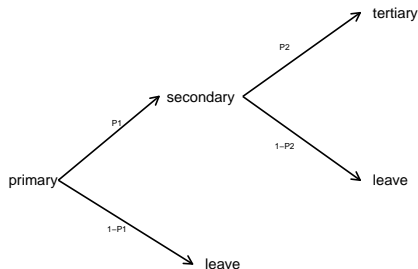
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  - ▶ the Mare model (after Mare 1981)
- ▶ The aim of this talk is assess how sensitive the conclusions from this model are to unobserved heterogeneity.

## The sequential logit model



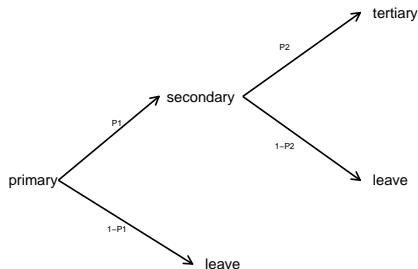
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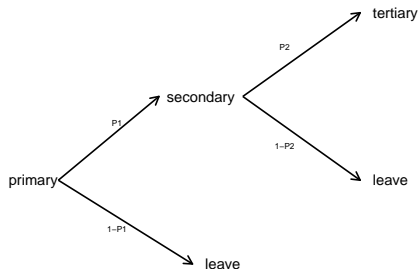
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- ▶  $p_1 = \Lambda(\beta_{01} + \beta_{11}X + \beta_{21}Z)$
- ▶  $p_2 = \Lambda(\beta_{02} + \beta_{12}X + \beta_{22}Z)$

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- ▶  $\Lambda(u) = \frac{\exp(u)}{1+\exp(u)}$



# Outline

The problem

A solution

An application

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  - ▶ The Averaging Mechanism
  - ▶ The Selection Mechanism

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- ▶ This means that the unobserved variable is likely to become a confounding variable at higher transitions, even if it was not one at the first transition

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- ▶ These scenarios are not intended to be true, but together they are meant to show what unobserved heterogeneity could do to the estimates.
- ▶ A sensitivity analysis is intended to show which conclusions are robust and which are not.



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- ▶ The scenarios can differ with respect to the initial standard deviation of  $\varepsilon$  and the initial correlation between  $x$  and  $\varepsilon$
- ▶ This standard deviation can be seen as the effect of a standardized version of  $\varepsilon$ .
- ▶ The effect of  $x$  given a scenario can be computed in Stata using the `seqlogit` package.

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- ▶ father's occupation measured in ISEI scores.
- ▶ both are standardized.

## Sequential logit model for the Netherlands (Males)

	primary versus lower secondary	lower secondary versus higher secondary	higher secondary versus tertiary
father's education	1.442 (11.51)	0.713 (11.79)	0.447 (7.13)
father's education X cohort	-0.117 (-4.82)	-0.026 (-2.34)	-0.031 (-2.80)
father's occupation	0.814 (13.06)	0.455 (8.15)	0.226 (3.37)
father's occupation x cohort	-0.087 (-6.32)	-0.016 (-1.53)	0.015 (1.28)
<i>N</i>	42271		

log odds ratios, z statistics in parentheses

# Scenarios

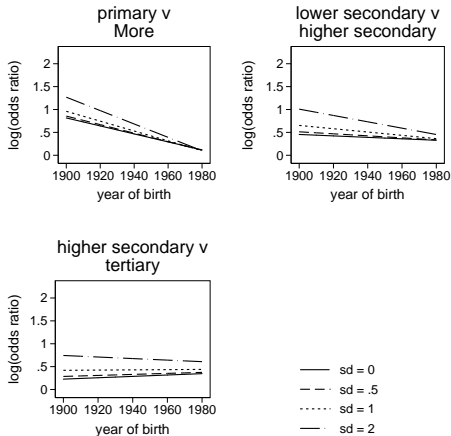
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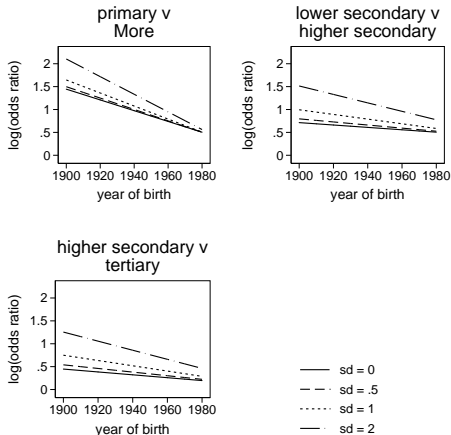
- ▶ The standard deviation of  $\varepsilon$  ranges from .5 to 5.
- ▶ The correlation between  $\varepsilon$  and father's education or occupation ranges from -.60 to .60.



## Effect of father's occupation in various scenarios



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## Two conclusions

decline of the effect of father's education and occupation over cohorts

p-values,  $H_0: \text{trend} \geq 0$

	father's education	father's occupation
transition 1	.000	.000
transition 2	.010	.063
transition 3	.003	.900

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decline of the effect of father's education and occupation over transitions

p-value,  $H_0: \text{father's resource is equal across transitions}$

father's education	father's occupation
.000	.000

# H0: effect father's education equal across transitions

p-values

		sd									
		.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
corr	-.60	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.002	0.003
	-.50	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.002	0.003
	-.40	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.003	0.004
	-.30	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.002	0.003	0.004
	-.25	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.002	0.003	0.004
	-.20	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.002	0.003	0.004
	-.15	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.002	0.003	0.005
	-.10	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.002	0.004	0.005
	-.05	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.003	0.004	0.005
	0	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.003	0.004	0.005
	.05	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.003	0.004	0.005
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	.30	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.002	0.003	0.004
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.50	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.002	0.003	
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# H0: effect father's occupation equal across transitions

p-values

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		.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
corr	-.60	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.003	0.005	0.006
	-.50	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.004	0.006	0.008
	-.40	0.000	0.000	0.000	0.000	0.001	0.002	0.003	0.005	0.007	0.009
	-.30	0.000	0.000	0.000	0.000	0.001	0.002	0.004	0.006	0.008	0.010
	-.25	0.000	0.000	0.000	0.000	0.001	0.002	0.004	0.006	0.008	0.010
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	.40	0.000	0.000	0.000	0.000	0.001	0.002	0.003	0.005	0.007	0.009
.50	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.004	0.006	0.008	
.60	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.003	0.005	0.006	

# H0: Trend effect father's education in transition 1 $\geq 0$

p-values

		sd									
		.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
corr	-.60	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.50	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
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.50	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	
.60	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	

# H0: Trend effect father's education in transition 2 $\geq 0$

p-values

		sd									
		.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
corr	-.60	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.50	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.40	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
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.60	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	



# H0: Trend effect father's education in transition 3 $\geq 0$

p-values

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	-.50	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.40	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.30	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.25	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.20	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.15	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.10	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.05	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.05	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.10	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.15	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.20	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.25	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.30	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.40	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
.50	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	
.60	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	

# H0: Trend effect father's occupation in transition $1 \geq 0$

p-values

		sd									
		.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
corr	-.60	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.50	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.40	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.30	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.25	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.20	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.15	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.10	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.05	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.05	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.10	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.15	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.20	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.25	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.30	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.40	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
.50	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	
.60	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	

# H0: Trend effect father's occupation in transition 2 $\geq 0$

p-values

		sd									
		.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
corr	-.60	0.031	0.005	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.50	0.028	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.40	0.025	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.30	0.023	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.25	0.023	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.20	0.022	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.15	0.022	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.10	0.021	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	-.05	0.021	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	0	0.021	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.05	0.021	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.10	0.021	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.15	0.022	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.20	0.022	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.25	0.023	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.30	0.023	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	.40	0.025	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
.50	0.028	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	
.60	0.031	0.005	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	

# H0: Trend effect father's occupation in transition $3 \geq 0$

p-values

		sd									
		.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
corr	-.60	0.846	0.681	0.464	0.286	0.171	0.104	0.066	0.044	0.031	0.023
	-.50	0.836	0.645	0.414	0.241	0.139	0.083	0.052	0.035	0.025	0.019
	-.40	0.828	0.618	0.378	0.212	0.119	0.070	0.044	0.030	0.021	0.016
	-.30	0.822	0.597	0.353	0.192	0.106	0.062	0.039	0.026	0.019	0.015
	-.25	0.820	0.589	0.344	0.185	0.102	0.059	0.037	0.025	0.018	0.014
	-.20	0.818	0.583	0.336	0.180	0.098	0.057	0.036	0.024	0.018	0.014
	-.15	0.816	0.578	0.331	0.176	0.096	0.056	0.035	0.024	0.018	0.014
	-.10	0.815	0.574	0.327	0.173	0.094	0.055	0.034	0.023	0.017	0.013
	-.05	0.815	0.572	0.325	0.172	0.093	0.054	0.034	0.023	0.017	0.013
	0	0.814	0.572	0.324	0.171	0.093	0.054	0.034	0.023	0.017	0.013
	.05	0.815	0.572	0.325	0.172	0.093	0.054	0.034	0.023	0.017	0.013
	.10	0.815	0.574	0.327	0.173	0.094	0.055	0.034	0.023	0.017	0.013
	.15	0.816	0.578	0.331	0.176	0.096	0.056	0.035	0.024	0.018	0.014
	.20	0.818	0.583	0.336	0.180	0.098	0.057	0.036	0.024	0.018	0.014
	.25	0.820	0.589	0.344	0.185	0.102	0.059	0.037	0.025	0.018	0.014
	.30	0.822	0.597	0.353	0.192	0.106	0.062	0.039	0.026	0.019	0.015
	.40	0.828	0.618	0.378	0.212	0.119	0.070	0.044	0.030	0.021	0.016
.50	0.836	0.645	0.414	0.241	0.139	0.083	0.052	0.035	0.025	0.019	
.60	0.846	0.681	0.464	0.286	0.171	0.104	0.066	0.044	0.031	0.023	

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  - ▶ both the effect and the trend are likely to be underestimated
  - ▶ most conclusions are robust
  - ▶ the exception is the non-significant trend in the effect of father's occupation in the second transition.

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## Observe IQ

transition	IQ	class	y		N	Pr(pass)	odds(pass)	log odds ratio
			fail	pass				
1	low	low	300	100	400			
		high	200	200	400			
	high	low	200	200	400			
		high	100	300	400			
2	low	low	75	25	100			
		high	100	100	200			
	high	low	100	100	200			
		high	75	225	300			

## Not observe IQ

transition	x	y		N	Pr	odds	log odds ratio
		fail	pass				
1	low	500	300	800			
	high	300	500	800			
2	low	175	125	300			
	high	175	325	500			

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			fail	pass				
1	low	low	300	100	400			
		high	200	200	400			
	high	low	200	200	400			
		high	100	300	400			
2	low	low	75	25	100			
		high	100	100	200			
	high	low	100	100	200			
		high	75	225	300			

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	high	175	325	500			



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		high	200	200	400			
	high	low	200	200	400			
		high	100	300	400			
2	low	low	75	25	100			
		high	100	100	200			
	high	low	100	100	200			
		high	75	225	300			

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	high	300	500	800			
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	high	175	325	500			

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			fail	pass				
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		high	200	200	400			
	high	low	200	200	400			
		high	100	300	400			
2	low	low	75	25	100			
		high	100	100	200			
	high	low	100	100	200			
		high	75	225	300			

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transition	x	y		N	Pr	odds	log odds ratio
		fail	pass				
1	low	500	300	800			
	high	300	500	800			
2	low	175	125	300			
	high	175	325	500			

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1	low	low	300	100	400			
		high	200	200	400			
	high	low	200	200	400			
		high	100	300	400			
2	low	low	75	25	100			
		high	100	100	200	200		
	high	low	100	100	200			
		high	75	225	300	300		

## Not observe IQ

transition	x	y		N	Pr	odds	log odds ratio
		fail	pass				
1	low	500	300	800			
	high	300	500	800			
2	low	175	125	300			
	high	175	325	500			

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			fail	pass				
1	low	low	300	100	400			
		high	200	200	400			
	high	low	200	200	400			
		high	100	300	400			
2	low	low	75	25	100			
		high	100	100	200			
	high	low	100	100	200			
		high	75	225	300			

## Not observe IQ

transition	x	y		N	Pr	odds	log odds ratio
		fail	pass				
1	low	500	300	800			
	high	300	500	800			
2	low	175	125	300			
	high	175	325	500			

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transition	IQ	class	y		N	Pr(pass)	odds(pass)	log odds ratio
			fail	pass				
1	low	low	300	100	400			
		high	200	200	400			
	high	low	200	200	400			
		high	100	300	400			
2	low	low	75	25	100			
		high	100	100	200			
	high	low	100	100	200			
		high	75	225	300			

## Not observe IQ

transition	x	y		N	Pr	odds	log odds ratio
		fail	pass				
1	low	500	300	800			
	high	300	500	800			
2	low	175	125	300			
	high	175	325	500			

## Observe IQ

transition	IQ	class	y		N	Pr(pass)	odds(pass)	log odds ratio
			fail	pass				
1	low	low	300	100	400	0.25		
		high	200	200	400	0.5		
	high	low	200	200	400	0.5		
		high	100	300	400	0.75		
2	low	low	75	25	100	0.25		
		high	100	100	200	0.5		
	high	low	100	100	200	0.5		
		high	75	225	300	0.75		

## Not observe IQ

transition	x	y		N	Pr	odds	log odds ratio
		fail	pass				
1	low	500	300	800	0.375		
	high	300	500	800	0.625		
2	low	175	125	300	0.417		
	high	175	325	500	0.65		

## Observe IQ

transition	IQ	class	y		N	Pr(pass)	odds(pass)	log odds ratio
			fail	pass				
1	low	low	300	100	400	0.25	0.333	
		high	200	200	400	0.5	1	
	high	low	200	200	400	0.5	1	
		high	100	300	400	0.75	3	
2	low	low	75	25	100	0.25	0.333	
		high	100	100	200	0.5	1	
	high	low	100	100	200	0.5	1	
		high	75	225	300	0.75	3	

## Not observe IQ

transition	x	y		N	Pr	odds	log odds ratio
		fail	pass				
1	low	500	300	800	0.375	0.6	
	high	300	500	800	0.625	1.667	
2	low	175	125	300	0.417	0.714	
	high	175	325	500	0.65	1.857	

## Observe IQ

transition	IQ	class	y		N	Pr(pass)	odds(pass)	log odds ratio
			fail	pass				
1	low	low	300	100	400	0.25	0.333	log(3)
		high	200	200	400	0.5	1	
	high	low	200	200	400	0.5	1	log(3)
		high	100	300	400	0.75	3	
2	low	low	75	25	100	0.25	0.333	log(3)
		high	100	100	200	0.5	1	
	high	low	100	100	200	0.5	1	log(3)
		high	75	225	300	0.75	3	

## Not observe IQ

transition	x	y		N	Pr	odds	log odds ratio
		fail	pass				
1	low	500	300	800	0.375	0.6	log(2.778)
	high	300	500	800	0.625	1.667	
2	low	175	125	300	0.417	0.714	log(2.6)
	high	175	325	500	0.65	1.857	